MODELLING PROBLEMS #2

Consider the "arrested topographic wave" problem:

$$\zeta_{y} + \frac{r}{fs}\zeta_{xx} = 0$$

$$\zeta_{x} = \frac{Ff}{rg} \text{ at } x = 0$$

$$\zeta = 0 \text{ at } x \to \infty$$

where r = 0.1 cm/sec, s = 0.001, $f = 10^{-4}$ sec.

Solve two problems:

a)
$$F = 0$$
, $\zeta = \begin{cases} 10 \text{ cm} & 0 \le x \le 50 \text{ km} \\ 0 & x \ge 50 \text{ km} \end{cases}$;

b) F = -1 cm²/sec²,
$$\zeta(x,0) = 0$$

Solve numerically for ζ at -500 km < y < 0 in each problem using both the forward time/centered space scheme and the fully implicit scheme.